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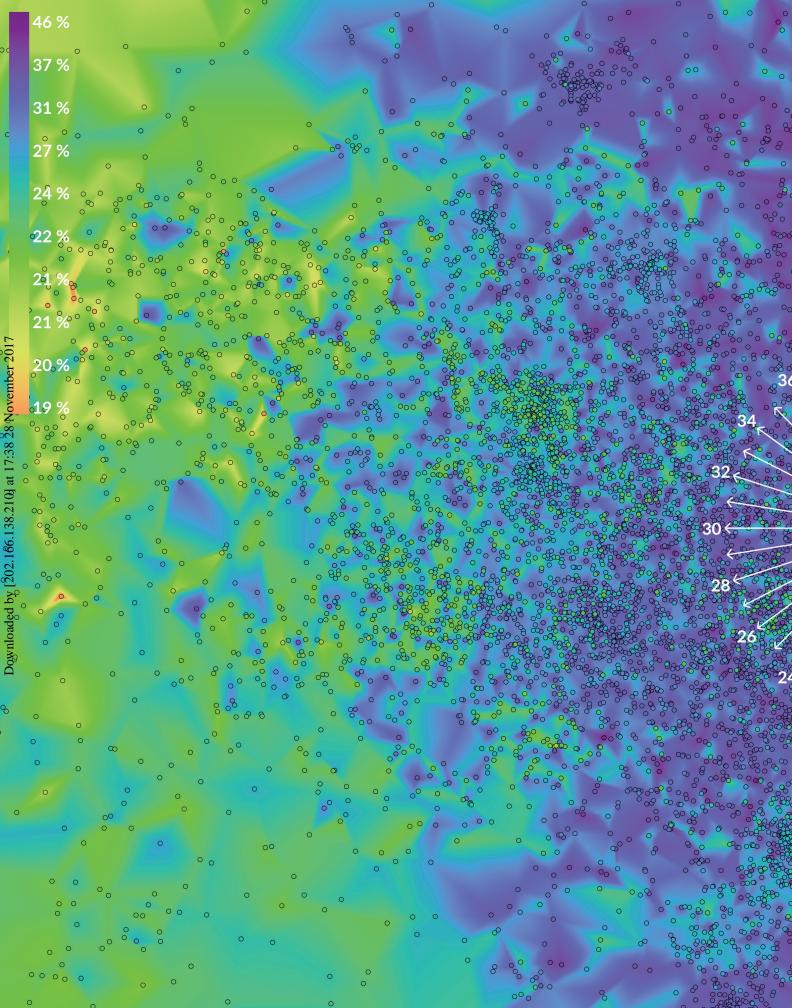


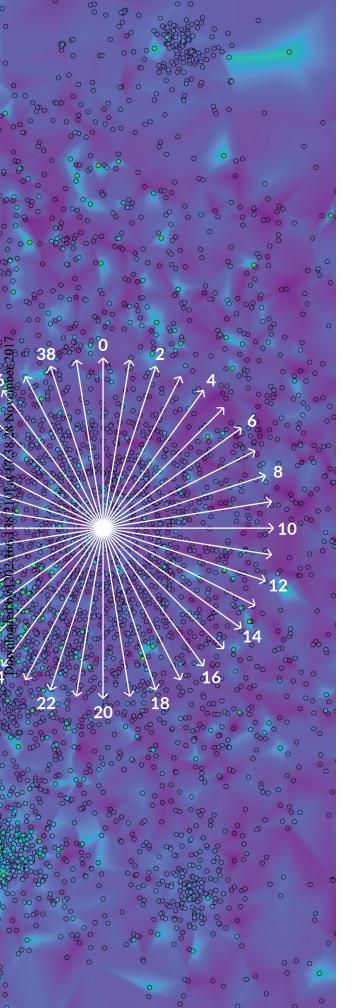
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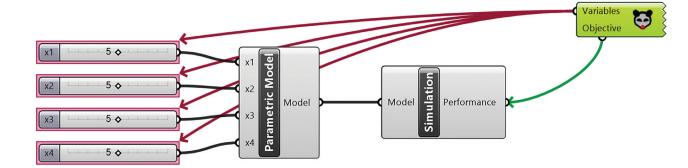




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## Model-based Optimization for Architectural Design: Optimizing Daylight and Glare in Grasshopper

Model-based optimization is an innovative optimization strategy and particularly appropriate for time-intensive performance simulations. To demonstrate this appropriateness, this paper reviews simulation-based optimization algorithms and benchmarks several (single- and multi-objective) optimization tools on two problems involving annual daylight and glare simulations. The benchmarks demonstrate that model-based optimization outperforms other (single- and multi-objective) approaches on time-intensive, simulationbased optimization problems and thus puts new applications within reach. In this way, model-based optimization aids architectural designers and consultants to develop more resource- and energy-efficient buildings.



#### Introduction and Background

Structural, building energy, and daylighting simulations play a key role in architectural design processes. They allow the quantitative evaluation of design variants, while parametric modeling allows the fast and automated generation of design variants from numerical parameters.<sup>1</sup> When designers combine parametric models with performance simulations, optimization algorithms find well-performing design variants. Consequently, simulation-based optimization is increasingly applied in leading architectural and engineering practices such as SOM<sup>2</sup> and ARUP<sup>3</sup> and was, for example, used in the design of the Louvre Abu Dhabi.<sup>4</sup>

Model-based optimization is an innovative, machine learning-related optimization strategy and particularly appropriate for time-intensive performance simulations. To demonstrate this appropriateness, this paper benchmarks several optimization tools in Grasshopper—a popular software for parametric design and performance simulations—on two problems involving annual daylight and, for one problem, glare simulations. These benchmarks include the first freely available, model-based optimization tool aimed at architectural design optimization (ADO), Opossum (OPtimizatiOn Solver with SUrrogate Models), of which the author is the lead developer. (Opossum is available as a free download at www.food4rhino.com/app/opossum-optimization-solver-surrogate-models.)

Model (or surrogate)-based optimization methods find good results with small numbers of simulations.<sup>5</sup> This high speed of convergence is important for sustainable design problems such as daylighting and building energy, where a single simulation takes several minutes or hours to complete. Under such conditions, it is impractical to perform the thousands of simulations required by population-based metaheuristics such as genetic algorithms (GAs).

#### Global Black-Box Optimization

Unlike the majority of optimization methods, global black-box (or derivative-free) methods do not need mathematical formulations of optimization problems and—unlike local optimization methods—do not get trapped in local optima but instead consider the whole design space.

Accordingly, they are appropriate for simulation-based optimization problems in ADO. Such problems define the relationship between variables and performance objectives not with a formula but by evaluating a parametric model with numerical simulations (Figure 2), and often exhibit local optima and complex interdependencies between variables.

Global black-box methods must compromise between exploring the design space as a whole with locally exploiting promising regions. They fall into three broad categories: Direct search, model-based methods, and metaheuristics. The following subsections discuss the three categories, before introducing Pareto-based optimization.

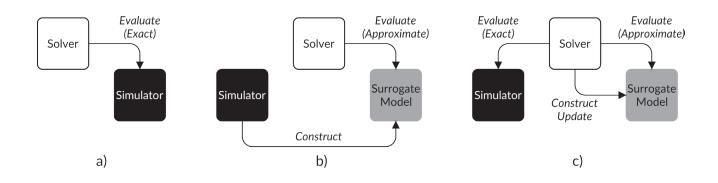
#### Direct Search

Direct search methods evaluate a deterministic sequence of solutions without trying to approximate the design space (Figure 3a). The well-known Hooke-Jeeves and Nelder-Mead Simplex algorithms are local direct search methods, while DIRECT<sup>6</sup> is a more recent, global method. DIRECT subdivides the design space into hyper-boxes and

✓ Figure 1 (Previous spread). Radial mapping of (most of) the simulated solutions for Problem 2. The position of every circle represents the solution's parameters, and the color its performance in terms of a weighted sum of daylight and glare, on a logarithmic scale. The background colors are interpolated with barycentric coordinates.

The better solutions on the left (<22%) indicate that the screen should be more porous on the top and less porous on the bottom (Figure 9). There are several very good (<20%) solutions that do not form a clear pattern, which indicates several distinct screen designs that are close to optimal.

Figure 3. Three types of simulation-based, black-box optimization: (a) Optimize the output of the exact simulation directly, (b) optimize the approximating output of the surrogate model constructed from prior simulation results, and (c) optimize and update the surrogate model during the optimization process.



excludes hyper-boxes from further subdivision by approximating the maximum change of the performance objective for each box (Figure 4). This paper presents results for DIRECT as implemented in the free, open-source NLopt library.<sup>7</sup>

#### Model-based Methods

Model-based methods approximate the design space as a whole by constructing surrogate models of the implicit mathematical formulations of simulation-based problems. Surrogate models are much faster to calculate than simulations and can accelerate optimization processes. However, as approximations, surrogate models are less accurate than the underlying simulations.

Accuracy is a concern especially for approaches that completely replace time-intensive simulations with surrogate models and then apply optimization (Figure 3b). Improving the models' accuracy requires a larger sample size, which can negate the initial speed advantage.

In contrast, model-based methods iteratively build and refine models during the optimization process (Figure 3c). At every iteration, a model-based method searches its model for a promising solution (deterministically, randomly, or with a metaheuristic). It simulates the found solution and updates the model with the exact simulation results (Figure 5). A model-based method thus improves its model's accuracy during the optimization process. For the second optimization problem discussed in the following section, the final models constructed by the model-based algorithm deviated at most 53% from the exact objective value, but only 11% on average.

Trust region methods employ local models, while more recent, global model-based methods approximate design spaces globally. Global methods construct surrogate models with a variety of statistical (e.g., Polynomial Regression and Kriging) and machine learning-related (e.g., Radial Basis Functions, Neural Networks and Support Vector Machines) techniques. Due to their ability to model complex design spaces, Kriging and radial basis functions are particularly suitable for simulation-based problems from engineering design<sup>8</sup> and, by extension, ADO. Opossum, the optimization tool presented here, interpolates design spaces with radial basis functions.<sup>9</sup>

Global model-based methods are particularly effective for optimizing problems with time-intensive simulations and complex relationships between variables and objective.<sup>10</sup> They converge—that is, find good solutions—quickly by alternating between evaluating the surrogate model, which is fast but approximate, and the exact simulation, which typically is much slower. The surrogate model not only improves convergence, but offers opportunities for visualization and interaction that are relevant for ADO.  $^{\rm 11}$ 

Compared to other types of optimization methods, model-based methods require additional calculations to construct and search the surrogate model at every optimization step. However, when a single function evaluation takes more than a few seconds, the time required for these calculations is negligible.<sup>12</sup>

This study considers the performance of RBFOpt,<sup>13</sup> a free and open-source, state-of-the-art library for model-based optimization powering Opossum. Of the twenty-eight solvers competing in the 2015 GECCO Black-Box Competition, which consisted of 1.000 mathematical benchmark problems with two to sixty-four variables, RBFOpt ranked seventh overall and first among the open-source solvers.<sup>14</sup>

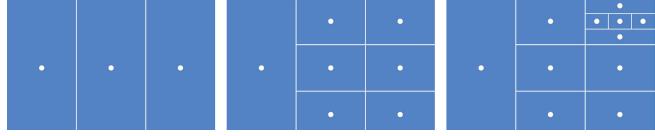
Based on previous benchmark results from building energy problems,<sup>15</sup> RBFOpt's continuously updated radial basis function model quickly identifies promising areas of the design space, but, in some cases, hinders the algorithm from focusing on promising areas. In other words, RBFOpt excels in global search but has weaknesses in local search. (RBFOpt v3.0.1, which dates from after the completion of the below experiments, addresses these weaknesses by incorporating a trust region method.)

RBFOpt is controlled by more than forty parameters. Depending on individual problem characteristics, some of these parameters drastically affect RBFOpt's performance.<sup>16</sup> The most importance choices are between different optimization (Gutmann<sup>17</sup> and MSRSM<sup>18</sup>) and interpolation methods. (RBFOpt v3.0.1 introduces automatic model selection as a default. With this setting, the algorithm tries to choose the most accurate interpolation method—linear, multi-quadratic, cubic and thin plate spline—for each problem.) Opossum's graphical user interface (GUI) reduces RBFOpt's complexity into three tabs that afford increasing levels of control (Figure 7) and offers presets that are based on intensive testing with mathematical test functions.

#### Metaheuristics

Stochastic, population-based metaheuristics<sup>19</sup> often are inspired by natural processes, such as genetic evolution or "swarm intelligence," and require extensive tuning of optimization parameters. Due to a lack of mathematical proofs of convergence and inferior performance on benchmarks,<sup>20</sup> the mathematical optimization community regards them as "methods of last resort."<sup>21</sup>

Nevertheless, metaheuristics are by far the most popular category of optimization methods in ADO, with GAs as the most



△ Figure 4. Diagram of three iterations of the DIRECT algorithm. Note how DIRECT subdivides promising regions of the design space while ignoring others.

△ Figure 5. Diagram of three iterations of a global, model-based algorithm. The dashed lines indicated the approximated design space.



 $\Delta$  Figure 6. Diagram of three iterations of a genetic algorithm.

prominent exponent.<sup>22</sup> Reasons for this popularity include a relative ease of implementation, wide availability, applicability to a wide range of problems, and a perception that metaheuristics are especially appropriate for complex, simulation-based problems.<sup>23</sup> This paper presents results for single- and multi-objective GAs, particle swarm optimization (PSO) and simulated annealing (SA).

GAs evolve a population of solutions through genetics-inspired operations (Figure 6), such as crossover, mutation, and selection. Schooling behaviors exhibited by, for example, birds and fish inspire PSO, where a "swarm" of solutions converges gradually in a good region of the space. SA considers only a single solution. Mimicking the movement of an atom in a cooling metal, the solution initially changes more randomly and stabilizes as the "temperature" drops.

#### Pareto-based Optimization

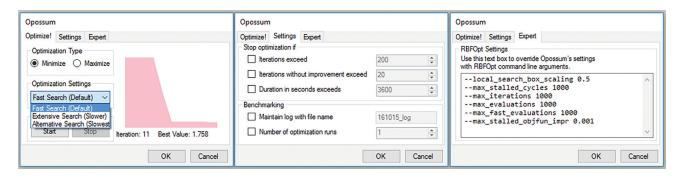
Pareto-based, multi-objective algorithms, which often are GAs, search for solutions that perform well in terms of more than one performance objective. This approach is popular in ADO, but less so in the mathematical optimization community, leading to a comparatively small number of optimization methods and benchmark results.

This paper considers a benchmark problem with the two objectives of daylight and glare, but combines the two into a single objective by subtracting them from each other. Alternatively, one can express multiple objectives as "soft constraints," for example, by penalizing the weight of a structure when it exceeds stress or deflection constraints.<sup>24</sup>

Pareto-based algorithms do not define such weighted or penalized sums, but instead optimize all objectives in parallel. Paretobased optimization is useful only when there is a tradeoff between objectives: for example, allowing more daylight into a room can lead to more glare. Pareto-based optimization explores such tradeoffs by searching for nondominated solutions, that is, solutions where improving one of the objectives is only possible by worsening others.

However, since Pareto-based optimization aims to not only find good solutions, but a set of nondominated solutions that represent different tradeoffs, it is less efficient than its single-objective counterpart. For example, in a benchmark of a building energy problem with two objectives, it took 1400–1800 function evaluations for the Pareto fronts to stabilize.<sup>25</sup>

The ADO literature does not address the efficiency difference between single- and multi-objective algorithms. For example, one paper characterizes Pareto-based optimization as "getting more for less" and mentions computation time only as a general limitation.<sup>26</sup> Similarly, a foundational paper perceives an affinity between



 $\Delta$  Figure 7. Opossum's GUI. The first tab lets users choose one of three pre-sets of parameters, and start and stop the optimization. The second tab provides options for benchmarking. The third tab offers full control by accepting command line parameters for RBFOpt.

the many tradeoffs addressed by architectural design and the comparatively smaller number of multiple objectives addressed by Pareto-based optimization, but acknowledges the performance tradeoffs of this approach only in a general sense.<sup>27</sup>

This paper speculates that architects often prefer Pareto-based optimization, because it offers a range of alternatives rather than a single result and not because it accurately represents trade-offs. It evaluates apples as oranges, and vice versa, by evaluating the Pareto-based GA HypE<sup>28</sup> as a single-objective algorithm and comparing the Pareto fronts found by HypE with the fronts found implicitly by the five single-objective algorithms.

#### **Optimizing Daylight and Glare**

To evaluate RBFOpt and Opossum, we compare its performance with the remaining global solvers available in Grasshopper: the GA and SA included in Galapagos,<sup>29</sup> the PSO of Silvereye,<sup>30</sup> the DIRECT algorithm included in Goat and HypE included in Octopus.<sup>31</sup> We test the solvers on two problems involving time-intensive daylighting simulations: optimizing a screened façade with discrete louver angles for daylight and optimizing a perforated façade with continuous opening sizes for daylight and glare. We simulate daylight and glare with DIVA-for-Rhino 4.0.<sup>32</sup>

#### Problem 1 (15 Discrete Variables)

The first optimization problem, defined by Wortmann et al.<sup>33</sup> and presented here with new and expanded benchmark results, considers a single room that is located on the Southwest corner of a building in Singapore (Figure 8).

The room has two facades, one with nine façade components and one with six. Every façade component has micro-louvers, which, for each façade component, can take angles between 0° and 180° (in increments of five). In other words, there are 37 daylightmodulating types of façade components.

The optimization problem aims to find a configuration of façade components that maximizes Useful Daylight Illuminance (UDI). UDI measures the annual percentage of time during which a sensor point receives an amount of daylight that is sufficient for office work, while avoiding glare and excessive heat gains (300–3000 lux). One simulates UDI via a grid of sensor points (Figures 8 and 9).<sup>34</sup>

In addition, we penalize configurations with angle differences larger than 10 degrees between neighboring façade components to ensure a coherent appearance of the façade and a subtle modulation of daylight. The penalty function in the following equation computes a penalty value pi for an individual façade component with angle di. If the angle difference with the previous neighbor is smaller than ten degrees, the penalty pi is zero; otherwise, it is a squared error term. The minimization objective is 100% minus average UDI u(x) plus the sum of the penalties of the fifteen façade components p(x):

 $pi(x) = \begin{cases} 0 \\ \left( \frac{|di-di-1|-10^{\circ}}{170^{\circ}} \right)^{2} \end{cases}^{di-di-1 \le 10^{\circ}}$ 

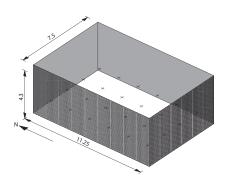
 $\min f(x) = 1.0 - \bar{u}(x) + \sum_{i=0}^{n} p_i(x)$ 

On an Intel Xeon E5-1620 CPU with sixteen threads and 3.6 GHz, one evaluation of this objective, that is, generating the parametric geometry and performing the daylighting simulation, takes about 75 seconds.

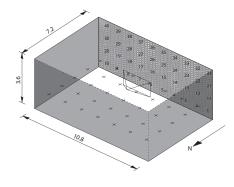
#### Problem 2 (40 Continuous Variables)

The second problem, defined by Wortmann<sup>35</sup> and presented here with a more rigorous comparison of the Pareto fronts, also considers a room in Singapore (Figure 9). The room has a southfacing façade, perforated by 1.692 openings of varying sizes. The continuous weights of a grid of forty attractor points, which are the problem's variables, controls these sizes and thus the façade's appearance and daylight performance.

This optimization problem aims to find a façade design that maximizes UDI and minimizes Daylight Glare Probability (DGP). DGP measures glare as a percentage for a specific camera view and point-in-time and classifies this percentage as imperceptible, perceptible, disturbing, or intolerable.<sup>36</sup> A recent evaluation of five glare indices concludes that all indices exhibit inaccuracies and inconsistencies. However, the authors state that "DGP shows



△ Figure 8. Diagram of the room optimized in terms of daylight. The crosses indicate the sensor grid for simulating UDI.



 $\triangle$  Figure 9. Diagram of the room optimized in terms of daylight and glare. The crosses indicate the sensor grid for simulating UDI and the cone the camera position and view for simulating DGP.

the best evaluation performance among the five indices" and that DGP "would be still very effective when we would like to find out whether or not discomfort glare exists," which is the case for the problem at hand.<sup>37</sup>

Although a more realistic glare assessment requires several camera views representing the users' true field of view, we calculate this value only for a single camera to hasten the many runs required for benchmarking. To further reduce calculation time, we approximate annual glare as an average of 59 representative daylight hours instead of a full annual glare simulation.<sup>38</sup> Although less accurate than a full annual simulation, this approach yields a good qualitative assessment of the presence or absence of discomfort glare.

Assuming that quality of daylight and avoidance of glare are equally important, subtracting average annual DGP g from average annual UDI u yields a single minimization objective (both UDI and DGP are in the range [0,1]):

### $\min f(x) = (1.0 - u(x) + g(x))/2$

On an Intel Xeon E5-1620 CPU with sixteen threads and 3.6 GHz, one simulation of UDI and approximated annual glare takes about 90 seconds.

#### Methodology

We optimize both problems for 200 function evaluations: ten times for each nondeterministic solver (RBFOpt, GA, SA, PSO, and HypE) and one time for the deterministic DIRECT.

Choice of parameters significantly affects the performance of optimization algorithms, especially for metaheuristics, and is problem-dependent.<sup>39</sup> Nevertheless, we assume sensible default parameter choices on part of the solvers' authors. Sensible defaults are important when, as in architectural practice, time pressure does not allow for extensive parameter tuning but calls for solvers that are efficient and immediately usable by nonexperts. Accordingly, we employ default parameters, except for the GA and HypE, where we halve the population sizes to 25 to achieve a larger number of generations.

Following standard benchmarking methodology, we evaluate the solvers relative to the number of function evaluations, that is, simulations, and not relative to running time. This methodology ensures the results' independence from computing speed and implementation details. In practice, compared to the time required for simulations, running time differences between solvers often are insignificant.

We employ two evaluation criteria: speed of convergence and stability. Speed of convergence, which is the more critical, measures how fast an algorithm approaches the optimum in terms of function evaluations. But repeated runs of stochastic algorithms for identical problems and settings can have dramatically different results. Stability, which is a concern for metaheuristics and other stochastic algorithms, is a statistical measure for an algorithm's reliability. Stability is important, because, in practice, one should not expect users to run an optimization algorithm more than once.

For problem 1, Octopus supplements the single objective with a second objective that aims to diversify the solution set found by HypE. In problem 2, we compare the Pareto-based solver with the single objective ones by calculating the weighted sum objective for the solutions found by HypE. We compare the singleobjective solvers with HypE by recording individual UDI and DGP values and calculating the resulting hypervolume. Hypervolume is a quality measure for Pareto fronts calculated as a percentage of the "covered" objective space based on the currently nondominated solutions.<sup>40</sup>

#### Results

The convergence graph on the left in Figure 10 depicts the average, current best value found by the solvers relative to the number of evaluations on problem 1. DIRECT is the best performing solver, and RBFOpt the second best. DIRECT finds

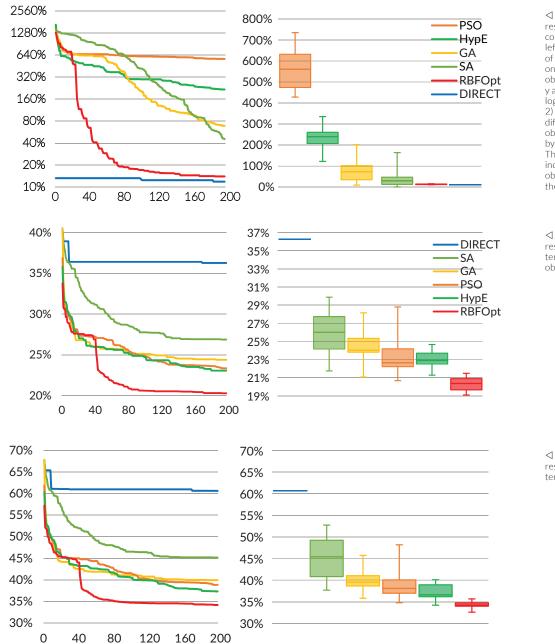


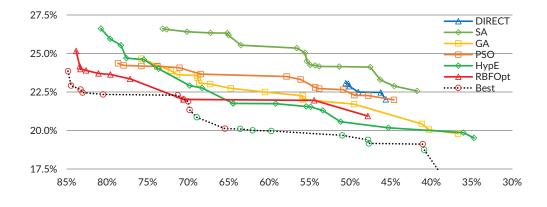
Figure 10. Benchmark  $\triangleleft$ results for problem 1. The convergence graph on the left displays the number of function evaluations on the x, and the average objective value on the v axis. The x axis is in logarithmic scale (base 2) to accommodate big differences between objective values caused by the penalty function. The box plot on the right indicates the range of objective values found by the six solvers in ten runs.

✓ Figure 11. Benchmark results for problem 2 in terms of the weighted objective function.

an excellent solution immediately, that is, it "gets lucky" in terms of its initialization sequence. Note RBFOpt's rapid progress after 15 evaluations: Here the algorithm starts profiting from the surrogate model, while the earlier evaluations sample the objective function with a quasi-random Latin Hypercube Design. The number of quasi-random samples is equal to the number of problem dimensions, i.e., variables. The remaining solvers perform poorly. The box plot on the right in Figure 10 indicates the range of objective values found by the solvers in ten runs.

On problem 2, DIRECT is the worst-performing solver because its recursive subdivision proceeds too slowly in the forty dimensions corresponding to the variables (Figure 11). SA performs comparatively poorly, while the remaining metaheuristics, including the Pareto-based HypE, perform similarly and improve the objective by around 40%. Opossum's RBFOpt is the best-performing solver with an improvement of 50%. For both problems, RBFOpt is the most stable nondeterministic algorithm.

Figure 12 graphs not the algorithms' objectives, but their hypervolumes. The results indicate that, on this problem, the singleobjective RBFOpt is more stable and finds more accurate Pareto fronts than the Pareto-based HypE. The curves in Figure 12 resembles the ones in Figure 11, since an improvement of the weighted



✓ Figure 13. Pareto fronts found during each solver's most representative (i.e., closest to the mean) run. "Best" is the combined front from all solvers and runs. The markers' color indicates the solver. UDI indicated on the x-, and average DGP indicated on the y-axis.

objective value implies an improvement of the Pareto front.

Figure 13 displays representative examples of Pareto fronts found by the solvers, which further illustrate the performance differences between them. Compared to HypE, RBFOpt has found a shallower front, that is, it has found better tradeoffs between maximizing daylight and minimizing glare, especially for high-daylight solutions. (Note that, although large improvements of daylight quality require only small increases in glare, low average DGP values can contain isolated instances of intolerable glare.)

#### Conclusion

The performance of optimization algorithms depends on the characteristics of individual optimization problems. Nevertheless, based on the benchmark results presented here and elsewhere<sup>41</sup> and results from the literature,<sup>42</sup> a rough, general recommendation can be made: Designers should apply metaheuristics primarily on problems where thousands, or tens of thousands, function evaluations are possible, direct search on problems with relatively small numbers of variables and model-based methods especially on problems with larger numbers of variables and limited function evaluation budgets. Accordingly, model-based methods are particularly attractive for ADO, where design problems often are complex and involve time-intensive simulations. For the complex and time-intensive daylighting problems presented here, Opossum's RBFOpt is the best choice overall.

The comparison with a Pareto-based algorithm indicates that designers should employ Pareto-based optimization judiciously and only when a large evaluation budget is available to avoid an inaccurate approximation of the Pareto front. Currently, model-based optimization methods are used only rarely in ADO,<sup>43</sup> but results like the ones presented here highlight their potential for optimizing building designs based on time-intensive, structural and environmental simulations.

Nevertheless, this study takes only a small step on the road to more in-depth and rigorous studies of the performance of optimization methods in ADO. Such studies will require a dramatically enlarged catalogue of simulation-based benchmark problems, (single- and multi-objective) optimization methods and results. Another research direction is the improved integration of ADO with architectural design processes, for example through more interactive optimization algorithms and more insightful visualizations of design and objective spaces.

#### Acknowledgement

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